Teacher:

Grade 7 Math

Week	Online Lesson	Book Pages	Date Due
April 13 – April 17	3.1 3.2	Pgs. 72-76 Pgs. 77-82	April 24th at 2pm
April 20 – April 24	3.3 Module 3 Quiz	Pgs. 83-88 Pg. 89	April 24 at Spill
April 27 – May 1	4.1 4.2	Pgs. 95-100 Pgs. 101-106	May 8 th at 3pm
May 4 - May 8	4.3 4.4	Pgs. 107-112 Pgs. 113-120	hay or at spin
May 11 – May 15	Module 4 Quiz 5.1	Pgs. 121 Pgs. 127-132	May 22 nd at 3nm
May 18 – May 22	5.2 5.3	Pgs. 133-138 Pgs. 139-146	
May 25 – May 29	Module 5 Quiz 6.1	Pgs. 147 Pgs. 153-160	lune 5 th at 3nm
June 1 – June 5	6.2 6.3	Pgs. 161-166 Pgs. 167-172	Sure 5 at Spin
June 8 – June 12	6.4 Module 6 Quiz	Pgs. 173-178 Pgs. 179	June 19 th at 3pm
June 15 – June 19	ТВА	TBA	

Note: We do not know when we will be returning to school, the schedule was created with a worst-case scenario of us not returning in mind; when we return to school plans will be adjusted again.

Do your best to complete all of the pages associated with each lesson. If you need any help, please reach out to your math teacher using Remind (information in below).

If you would like to join the appropriate class and ask your teachers a question, you may communicate via Remind. Communication to your teachers is available Monday thru Friday from 7:30am – 2:30pm.

- Mr. Zona to join his class is @zonamath7
- Ms. Molnar to join Grade 7 Math is @molnar2019
 - Mr. Aloian to join is @aloian207
 - Mrs. Nearhood to join Team 7A is @cluster7a
 - Mr. Wisniewski to join Team 7A is @LPS7b

Proportional Relationships



ESSENTIAL QUESTION

How can you use proportional relationships to solve real-world problems?



LESSON 3.1

Representing Proportional Relationships



LESSON 3.2

Rate of Change and Slope COMMON 8.F.4

LESSON 3.3

Interpreting the Unit Rate as Slope 8.EE.5, 8.F.2, 8.F.4



Real-World Video

Speedboats can travel at fast rates while sailboats travel more slowly. If you graphed distance versus time for both types of boats, you could tell by the steepness of the graph which boat was faster.





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Are / Ready?

Complete these exercises to review skills you will need for this module.

Write Fractions as Decimals

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EXAMPLE	$\frac{1.7}{2.5} = ?$	Multiply the numerator and the denominator by a power of 10 so that the denominator is a whole number. Write the fraction as a division problem. Write a decimal point and zeros in the dividend. Place a decimal point in the quotient. Divide as with whole numbers.	$\frac{1.7 \times 10}{2.5 \times 10} = \frac{17}{25}$
		Write the fraction as a division problem. Write a decimal point and zeros in the dividend. Place a decimal point in the quotient. Divide as with whole numbers.	$ \begin{array}{r} $

Write each fraction as a decimal.



Solve Proportions



 $\frac{5 \times 2}{7 \times 2} = \frac{x}{14}$ $\frac{7 \times 2}{14} = \frac{14}{14}$ $\frac{7 \times 2}{14} = \frac{14}{14}$

Solve each proportion for x.





Visualize Vocabulary

Use the ✔ words to complete the diagram.



Understand Vocabulary

Match the term on the left to the definition on the right.

1. unit rate

2. constant of

3. proportional

relationship

proportionality

variables related proportionally.

A. A constant ratio of two

- B. A rate in which the second quantity in the comparison is one unit.
- C. A relationship between two quantities in which the ratio of one quantity to the other quantity is constant.

Active Reading

Key-Term Fold Before beginning the module, create a key-term fold to help you learn the vocabulary in this module. Write the highlighted vocabulary words on one side of the flap. Write the definition for each word on the other side of the flap. Use the key-term fold to quiz yourself on the definitions used in this module.

Vocabulary

Review Words

constant (constante)

 equivalent ratios (razones equivalentes)

proportion (proporción) rate (tasa)

- ✓ ratios (razón)
- ✓ unit rates (tasas unitarias)

Preview Words

constant of proportionality (constante de proporcionalidad) proportional relationship (relación proporcional) rate of change (tasa de cambio) slope (pendiente)



MODULE 3 Unpacking the Standards

Understanding the standards and the vocabulary terms in the standards will help you know exactly what you are expected to learn in this module.

COMMON 8.EE.5

Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways.

Key Vocabulary

proportional relationship

(relación proporcional)

A relationship between two quantities in which the ratio of one quantity to the other quantity is constant.

slope (pendiente)

A measure of the steepness of a line on a graph; the rise divided by the run.

unit rate (tasa unitaria)

A rate in which the second quantity in the comparison is one unit.



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What It Means to You

You will use data from a table and a graph to apply your understanding of rates to analyzing real-world situations.

UNPACKING EXAMPLE 8.EE.5

The table shows the volume of water released by Hoover Dam over a certain period of time. Use the data to make a graph. Find the slope of the line and explain what it shows.



Water Released from Hoover Dam				
Time (s)Volume of water (ft³)				
5	75,000			
10	150,000			
15	225,000			
20	300,000			

Water Released from Hoover Dam



The slope of the line is 15,000. This means that for every second that passed, 15,000 ft³ of water was released from Hoover Dam.

Suppose another dam releases water over the same period of time at a rate of 180,000 ft³ per minute. How do the two rates compare?

180,000 ft³ per minute is equal to 3,000 ft³ per second. This rate is one fifth the rate released by the Hoover Dam over the same time period.



Lesson 3.1 71



Representing Proportional Relationships with Equations

The ratio of the distance in miles to the distance in leagues is constant. This relationship is said to be *proportional*. A **proportional relationship** is a relationship between two quantities in which the ratio of one quantity to the other quantity is constant.

A proportional relationship can be described by an equation of the form y = kx, where k is a number called the **constant of proportionality**.

Sometimes it is useful to use another form of the equation, $k = \frac{y}{x}$.



Representing Proportional Relationships with Graphs

You can represent a proportional relationship with a graph. The graph will be a line that passes through the origin (0, 0). The graph shows the relationship between distance measured in miles to distance measured in leagues.



COMMON

12 18 24 30

Earth weight (lb)

10

8

6

0

6

Moon weight (lb)

8.EE.6



STEP 1

The graph shows the relationship between the weight of an object on the Moon and its weight on Earth. Write an equation for this relationship.

Use the points on the graph to make a table.

Earth weight (lb)	6	12	18	30
Moon weight (lb)	1	2	3	5

STEP 2 Find the constant of proportionality.

 $\frac{\text{Moon weight}}{\text{Earth weight}} \qquad \frac{1}{6} = \frac{1}{6} \qquad \frac{2}{12} = \frac{1}{6} \qquad \frac{3}{18} = \frac{1}{6} \qquad \frac{5}{30} = \frac{1}{6}$

The constant of proportionality is $\frac{1}{6}$.

STEP 3 Write an equation.

Let *x* represent weight on Earth.

Let *y* represent weight on the Moon.

The equation is $y = \frac{1}{6}x$.

Replace k with $\frac{1}{6}$ in y = kx.

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The graph shows the relationship between the amount of time that a backpacker hikes and the distance traveled.

- 4. What does the point (5, 6) represent?
- 5. What is the equation of the relationship?





Lesson 3.1 **73**

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Guided Practice

1. Vocabulary A proportional relationship is a relationship between two quantities in which the ratio of one quantity to the other quantity

is / is not constant.

2. Vocabulary When writing an equation of a proportional relationship in the



- Write an equation that describes the proportional relationship between the number of days and the number of weeks in a given length of time. (Explore Activity and Example 1)
 - **a.** Complete the table.

Time (weeks)	1	2	4		10
Time (days)	7			56	

b. Let *x* represent _____

Let y represent ______.

The equation that describes the relationship is ______.

Each table or graph represents a proportional relationship. Write an equation that describes the relationship. (Example 1 and Example 2)

4. Physical Science The relationship between the numbers of oxygen atoms and hydrogen atoms in water is shown below.

Oxygen atoms	2	5		120
Hydrogen atoms	4		34	



ESSENTIAL QUESTION CHECK-IN

6. If you know the equation of a proportional relationship, how can you draw the graph of the equation?

3.1 Independent Practice

COMMON 8.EE.6, 8.F.4



Date_

The table shows the relationship between temperatures measured on the Celsius and Fahrenheit scales.

Class_

Celsius temperature	0	10	20	30	40	50
Fahrenheit temperature	32	50	68	86	104	122

- **7.** Is the relationship between the temperature scales proportional? Why or why not?
- **8.** Describe the graph of the Celsius-Fahrenheit relationship.
- **9.** Analyze Relationships Ralph opened a savings account with a deposit of \$100. Every month after that, he deposited \$20 more.
 - a. Why is the relationship described not proportional?
 - **b.** How could the situation be changed to make the situation proportional?
- **10.** Represent Real-World Problems Describe a real-world situation that can be modeled by the equation $y = \frac{1}{20}x$. Be sure to describe what each variable represents.

Look for a Pattern The variables x and y are related proportionally.

- **11.** When *x* = 8, *y* = 20. Find *y* when *x* = 42.
- **12.** When *x* = 12, *y* = 8. Find *x* when *y* = 12.

a. Use the points on the graph to make a table.

Distance (in.)			
Time (min)			

- **b.** Write the equation for the relationship and tell what each variable represents.
- c. How long does it take the snail to crawl 85 inches?



FOCUS ON HIGHER ORDER THINKING

14. Communicate Mathematical Ideas Explain why all of the graphs in this lesson show the first quadrant but omit the other three quadrants.

15. Analyze Relationships Complete the table.

Length of side of square	1	2	3	4	5
Perimeter of square					
Area of square					

- **a.** Are the length of a side of a square and the perimeter of the square related proportionally? Why or why not?
- **b.** Are the length of a side of a square and the area of the square related proportionally? Why or why not?
- **16.** Make a Conjecture A table shows a proportional relationship where *k* is the constant of proportionality. The rows are then switched. How does the new constant of proportionality relate to the original one?

Work Area



Snail Crawling





Lesson 3.2 77



COMMON 8.F.4

You can also use a graph to find rates of change.

The graph shows the distance Nathan bicycled over time. What is Nathan's rate of change?



Reflect

- **2.** Make a Conjecture Does a proportional relationship have a constant rate of change?
- **3.** Does it matter what interval you use when you find the rate of change of a proportional relationship? Explain.



Calculating Slope m

When the rate of change of a relationship is constant, any segment of its graph has the same steepness. The constant rate of change is called the *slope* of the line.



COMMON CORE 8.F.4



My Notes

Slope Formula

The **slope** of a line is the ratio of the change in *y*-values (rise) for a segment of the graph to the corresponding change in *x*-values (run).

 $m = \frac{\mathbf{y}_2 - \mathbf{y}_1}{\mathbf{x}_2 - \mathbf{x}_1}$

EXAMPLE 2

Find *m*, the slope of the line.



Guided Practice



Class_



15. Multiple Representations Graph parallelogram *ABCD* on a coordinate plane with vertices at A(3, 4), B(6, 1), C(0, -2), and D(-3, 1).

b. What do you notice about the slopes?

a. Find the slope of each side.

- **c.** Draw another parallelogram on the coordinate plane. Do the slopes have the same characteristics?

FOCUS ON HIGHER ORDER THINKING

16. Communicate Mathematical Ideas Ben and Phoebe are finding the slope of a line. Ben chose two points on the line and used them to find the slope. Phoebe used two different points to find the slope. Did they get the same answer? Explain.

17. Analyze Relationships Two lines pass through the origin. The lines have slopes that are opposites. Compare and contrast the lines.

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Work Area

18. Reason Abstractly What is the slope of the *x*-axis? Explain.

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Practice

 Select any two pairs of points on the line graphed, draw corresponding right triangles indicating the rise and run for each pair, and show that the slope is the same between the two pairs of points.



2. The same line is used below to generate different triangles. Verify that the slope ratios are the same for all the triangles generated by points on this line.



Use slope to determine whether the given points are all on the same line.

3. (-6, -2), (0, -5), (2, -6)

- **4.** (-10, -2), (-5, 0), (10, 6)
- **5.** A line passes through the point (0, 0) and has a *rise* over *run* ratio of $\frac{4}{3}$. Give two other points that the line passes through.
- **6.** A wheelchair ramp is allowed a maximum of one inch of rise for every foot of run. Give the dimensions of three different wheelchair ramps that would meet this requirement.





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Using Slopes to Compare Unit Rates

You can compare proportional relationships presented in different ways.

EXAMPLE 2

COMMON 8.EE.5, 8.F.2

Well B Pumping Rate

10

Time (h)

20

20

0

Amount (barrels)





barrels per hour, that oil is pumped from Well A. The graph represents the rate that oil is pumped from Well B. Which well pumped oil at a faster rate? **STEP 1** Use the equation y = 2.75x to make

The equation y = 2.75x represents the rate, in

Use the equation y = 2.75x to make a table for Well A's pumping rate, in barrels per hour.

 Time (h)
 1
 2
 3
 4

 Quantity (barrels)
 2.75
 5.5
 8.25
 11

STEP 2

Use the table to find the slope of the graph of Well A.

slope = unit rate = $\frac{5.5 - 2.75}{2 - 1} = \frac{2.75}{1} = 2.75$ barrels/hour

STEP 3 Use the graph to find the slope of the graph of Well B.

slope = unit rate =
$$\frac{rise}{run} = \frac{10}{4} = 2.5$$
 barrels/hour

STEP 4 Compare the unit rates.

2.75 > 2.5, so Well A's rate, 2.75 barrels/hour, is faster.

Reflect

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3. Describe the relationships among the slope of the graph of Well A's rate, the equation representing Well A's rate, and the constant of proportionality.



4. The equation y = 375x represents the relationship between x, the time that a plane flies in hours, and y, the distance the plane flies in miles for Plane A. The table represents the relationship for Plane B. Find the slope of the graph for each plane and the plane's rate of speed. Determine which plane is flying at a faster rate of speed.

Time (h)	1	2	3	4
Distance (mi)	425	850	1275	1700





1. Jorge: 5 miles every 6 hours

2. Akiko



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3.3 Independent Practice

COMMON 8.EE.5, 8.F.2, 8.F.4

- 7. A Canadian goose migrated at a steady rate of 3 miles every 4 minutes.
 - **a.** Fill in the table to describe the relationship.

Time (min)	4	8			20
Distance (mi)			9	12	

b. Graph the relationship.



c. Find the slope of the graph and describe what it means in the context of this problem.

8. Vocabulary A unit rate is a rate in which the

first quantity / second quantity in the comparison is one unit.

Class

9. The table and the graph represent the rate at which two machines are bottling milk in gallons per second.



- Determine the slope and unit rate of each machine. a.
- **b.** Determine which machine is working at a faster rate.







10. Cycling The equation $y = \frac{1}{9}x$ represents the distance y, in kilometers, that Patrick traveled in x minutes while training for the cycling portion of a triathlon. The table shows the distance y Jennifer traveled in x minutes in her training. Who has the faster training rate?

Time (min)	40	64	80	96
Distance (km)	5	8	10	12

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FOCUS ON HIGHER ORDER THINKING

11. Analyze Relationships There is a proportional relationship between minutes and dollars per minute, shown on a graph of printing expenses. The graph passes through the point (1, 4.75). What is the slope of the graph? What is the unit rate? Explain.

12. Draw Conclusions Two cars start at the same time and travel at different constant rates. A graph for Car A passes through the point (0.5, 27.5), and a graph for Car B passes through (4, 240). Both graphs show distance in miles and time in hours. Which car is traveling faster? Explain.

13. Critical Thinking The table shows the rate at which water is being pumped into a swimming pool.

Time (min)	2	5	7	12
Amount (gal)	36	90	126	216

Use the unit rate and the amount of water pumped after 12 minutes to find how much water will have been pumped into the pool after $13\frac{1}{2}$ minutes. Explain your reasoning.

Work Area

MODULE QUIZ

Ready to Go On?

3.1 Representing Proportional Relationships

 Find the constant of proportionality for the table of values.

x	2	3	4	5
у	3	4.5	6	7.5

 Phil is riding his bike. He rides 25 miles in 2 hours, 37.5 miles in 3 hours, and 50 miles in 4 hours. Find the constant of proportionality and write an equation to describe the situation.

3.2 Rate of Change and Slope

Find the slope of each line.





3.3 Interpreting the Unit Rate as Slope

5. The distance Train A travels is represented by d = 70t, where d is the distance in kilometers and t is the time in hours. The distance Train B travels at various times is shown in the table. What is the unit rate of each train? Which train is going faster?

Time (hours)	Distance (km)
2	150
4	300
5	375

ESSENTIAL QUESTION

6. What is the relationship among proportional relationships, lines, rates of change, and slope?

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MODULE 3 MIXED REVIEW Assessment Readiness



Selected Response

- **1.** Which of the following is equivalent to 5⁻¹?
 - (A) 4 (C) $-\frac{1}{5}$
 - **(B)** $\frac{1}{5}$ **(D)** -5
- **2.** Prasert earns \$9 an hour. Which table represents this proportional relationship?

A	Hours	4	6	8		
	Earnings (\$)	36	54	72		
₿	Hours	4	6	8		
	Earnings (\$)	36	45	54		
©	Hours	2	3	4		
	Earnings (\$)	9	18	27		
D	Hours	2	3	4		
	Earnings (\$)	18	27	54		

- **3.** A factory produces widgets at a constant rate. After 4 hours, 3,120 widgets have been produced. At what rate are the widgets being produced?
 - (A) 630 widgets per hour
 - (B) 708 widgets per hour
 - © 780 widgets per hour
 - D 1,365 widgets per hour
- 4. A full lake begins dropping at a constant rate. After 4 weeks it has dropped 3 feet. What is the unit rate of change in the lake's level compared to its full level?
 - (A) 0.75 feet per week
 - (B) 1.33 feet per week
 - \bigcirc -0.75 feet per week
 - ⑦ −1.33 feet per week

5. What is the slope of the line below?



6. Jim earns \$41.25 in 5 hours. Susan earns \$30.00 in 4 hours. Pierre's hourly rate is less than Jim's, but more than Susan's. What is his hourly rate?

(A) \$6.50	(C) \$7.35
B \$7.75	D \$8.25

Mini-Task

- Joelle can read 3 pages in 4 minutes,
 4.5 pages in 6 minutes, and 6 pages in 8 minutes.
 - **a.** Make a table of the data.

Minutes		
Pages		

- **b.** Use the values in the table to find the unit rate.
- **c.** Graph the relationship between minutes and pages read.

